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# THE STUDY OF THE INTERACTION OF INTENSE PICOSECOND LIGHT PULSE WITH MATERIALS

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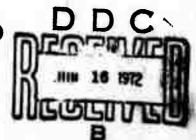
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# INVESTIGATION OF LASER ACTION IN GaAs WITH TWO PHOTON PUMP

by

Young Ho Park\* and Chi H. Lee

\*This is a M.S. Thesis of Mr. Young Ho Park. It is submitted to the Faculty of the Graduate School of the University of Maryland in partial fulfillment of the requirements for the degree of Master of Science, 1972.

#### ABSRTACT

Title of Thesis: Investigation of Laser Action in GaAs with Two Photon Pump

Name of Candidate: Young Ho Park

Thesis directed by: C.H. Lee, Assistant Professor

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by Young Ho Park

Thesis submitted to the Faculty of the Graduate School, of the University of Maryland in partial fulfillment of the requirements for the degree of Master of Science

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#### CHAPTER I

#### INTRODUCTION

The advent of intense coherent optical sources has made it experimentally feasible to observe multiphoton absorption in a number of materials. Two photon absorption in semiconductors can be employed to generate electron-hole pairs resulting in population inversion. Such a two photon pump could be used to observe laser action in bulk semiconductors. The laser action (1),(2),(3) in various bulk semiconductors such as GaAs, CdTe, CdSe, CdS, ZnS etc. have been investigated.

In the present experiment, the laser action in GaAs using a Nd:glass laser as a two photon pump was investigated with external mirrors forming the optical cavity. Such a bulk GaAs laser using external mirrors as resonator could be used to produce intense Q-switched optical pulses.

Even though the general theory for two photon absorption was first given by Maria Göppert-Mayer (4) in the Göttinger dissertation in 1931, the first observation of two photon absorption was made in 1961 by Kaiser and Garrett (5). Moreover the observation of two photon absorption in semiconductors came later. Braunstein and Ockman (2) observed two photon absorption in CdS pumped by a ruby laser. Basov (1) et al. investigated two photon absorption

in GaAs pumped by a Nd: glass laser and C. Chang (3) investigated two photon absorption for laser action in ZnS pumped by a ruby laser.

Before these observations, it had been thought that no optical transitions were possible which could create electron-hole pairs by absorbing photons possessing less energy than the energy gap. However, if the exciting source has sufficiently high power, many photons can be absorbed simultaneously. The absorption can be detected because the higher order nonlinear terms cannot be neglected.

In the present investigation we used GaAs, which has a band gap of 1.5 ev at 77°K and a Q-switched Nd:glass laser beam as pumping source. The latter has a photon energy of 1.17 ev. So the condition

2ħω > Eg > ħω

is satisfied where Eg is the energy gap of GaAs,  $\omega$  is angular frequency of the radiation of the laser,  $\hbar = \frac{h}{2\pi}$  and h is Planck's constant. If the semiconductor were purely intrinsic, only a two photon absorption process would be possible if we were to neglect higher order absorption. But in the experiment we do observe a single photon process when the pumping power is low. This is because of the single photon excitation of impurity levels in the forbidden band. According to the experimental result it is possible to distinguish one and two photon absorption process. Now this is a good

The transition probability for one and two photon absorption processes was calculated by Basov (1):

$$W^{(n)} \propto (n\hbar\omega - E_g)^{\frac{2\eta - 1}{2}} I^n \qquad \text{for } n = 1, 2$$

where hw: photon energy of pumping source beam

E<sub>e</sub>: energy gap of the semiconductor

I: intensity of pumping laser beam

w(n): upward transition probability per unit volume

The absorption coefficient  $K^{(n)}$  can be calculated as follows

$$K(u) = \frac{1}{M(u)} u u u$$

In a one-photon process

$$K^{(1)} \propto (\hbar \omega - E_3)^{1/2} = \text{const.},$$

but in a two-photon process

$$K^{(2)} \propto (2\hbar\omega - E_g)^{3/2} I = \text{const x } I$$
.

In a two photon process  $K^{(2)}$  is linearly proportional to the exciting laser intensity. In a one-photon process  $W^{(1)} \propto \operatorname{const} X I$  and in two photon process  $W^{(2)} \propto \operatorname{const} X I^2$ . As the intensities of the pumping source is increased, multiphoton absorption of light (in this case, two photon absorption of radiation in the semiconductors) becomes predominant.

At higher intensities  $K^{(2)}$  becomes much larger than  $K^{(1)}$ .

One of the most important features of the semiconductor

laser using two photon absorption is that the intensity

distribution inside the lasing crystal is more homogeneous

than that due to single photon absorption. This is obvious

conclusion of equations (2-1-13) and (2-1-14). Basov et al.

determined the intensity of light I(X) at penetration depth

X into the medium from the equation

$$\frac{dI}{dX} = -2\hbar\omega W^{(2)} - KI = -2\hbar\omega A I^2 - KI = -\beta I^2 - KI$$

where  $K=K^{(1)}$ ; single photon absorption coefficient .  $\beta=K^{(2)}/I=2\hbar\omega\lambda$   $W=\lambda I^{(2)}$ 

A; constant given in equation (2-1-11)From now on we will use W instead of W<sup>(2)</sup> since we are mainly interested in two photon process. The derivation of I(X) is shown in appendix III but the result is as follows

$$I(X) = \frac{I_0 \exp(-KX)}{1 + \frac{\beta I_0}{K} [1 - \exp(-KX)]}$$

where  $I_0 = I_S (1 - r)$ 

7.

Is: total intensity of the exciting radiation incident on the surface of the medium

r: the reflection coefficient .

If two photon absorption is dominant, so KX << 1, then

$$I(X) = \frac{I_0}{\beta X I_0 + 1}$$

This equation indicates that a large volume of the semiconducting medium has participated in the lasing action. This gives rise to a much larger power output and better coherence of radiation than from p-n junction lasers.

We have seen that electrons can be excited into the conduction band by absorbing two photons, thus creating electron-hole pairs. These electrons and holes can recombine to emit optical radiation commonly called recombination radiation.

If we introduce resonant reflectors to this semiconductor medium, we can get stimulated emission as well as spontaneous emission. The probabilities for spontaneous emission and stimulated emission were derived by Lasher and Stern (6), followed by a theoretical analysis by Dumke (7). In order to get the laser action in the semiconductor, it has to satisfy the population inversion condition and threshold condition.

Even though we know it is possible to get laser action, it is not easy to experimentally varify whether it is truly laser action. But the group in Levedev Physics Institute (1)

and others (8) proved it with several experimental results.

One of method is to determine the narrowing of the width of emission spectrum. Farfield pattern would also help to determine laser action. Accurate bandwidth measurement can be performed to make sure of the laser action.

We examined the narrowing of the linewidth of the emission spectrum. As we increased the power density of the pumping laser above threshold, the linewidth of the emission spectrum narrowed abruptly. This can be a criterion for lasing in the GaAs quantum generator. But even though the power density was below the threshold, the narrowing of the linewidth was observed. This can be explained as the super-radiance. The details are discussed in the next chapter.

#### CHAPTER II

#### THE THEORETICAL BACKGROUND

The transition probability and absorption coefficient of two photon process are derived. The threshold power density of the exciting radiation is calculated. Then the narrowing of the linewidth of emission spectra is discussed.

## §1. The Transition Probability and the Absorption Coefficient

In order to derive the absorption coefficient, it is necessary to calculate transition probability using time dependent perturbation theory. In the present investigation, the transition probability has to be calculated taking into account the band structure of GaAs. GaAs is a direct band gap semiconductor having a zinc sulfide structure. The band structure of such semiconductors have been extensively investigated by E.O. Kane (9). In the following we assume the band structure of GaAs as given by T.S. Moss (10) and calculate the transition probability and two photon absorption coefficient in GaAs.

First the Hamiltonian of the electron moving in the presence of an electromagnetic field can be written as

$$H = (\overline{P} + \frac{e}{c} \overline{A})^2/2m + V$$

$$H = \frac{1}{2m} \left( \overline{P} + \frac{e}{c} \overline{A} \right) \cdot \left( \overline{P} + \frac{e}{c} \overline{A} \right) + V$$

$$= \frac{P^2}{2m} + V + \frac{e}{2mc} \left( \overline{P} \cdot \overline{A} + \overline{A} \cdot \overline{P} \right) + \frac{e^2}{2mc^2} A^2$$

Since  $\overline{P}$  and  $\overline{A}$  commute if we choose the gauge such that  $\nabla \cdot \overline{A} = 0$ ,

$$H = \frac{P^2}{2m} + V + \frac{e}{mc} \cdot \overline{P} \cdot \overline{A} + \frac{e^2}{2mc^2} A^2 \qquad (2-1-1)$$

where P: momentum operator

A: vector potential

V: potential energy

m: mass of free electron

Let  $H_0 = \frac{p^2}{2m} + V$  be the unperturbed Hamiltonian. Then the term  $\frac{e}{mc} \cdot \overline{P} \cdot \overline{A} + \frac{e^2}{2mc^2} A^2$  can be regarded as a

perturbing term. But for one or two photon processes, the term  $\frac{e^2}{2mc^2}$   $A^2$  is much smaller than  $\frac{e}{mc}$   $\overline{P} \cdot \overline{A}$ . Figure

2-1-1 shows the band structure of GaAs. Gallium Arsenide has one conduction band and three valence bands. However in this experiment the transition probability from a valence band  $V_3$  to conduction band C is small compared to transition probability from  $V_1$  or  $V_2$  to C (Figure 2-1-1). Thus the transition probability from  $V_3$  to C can be neglected. In calculating the two photon transition probability, only the transition from  $V_1$  and  $V_2$  to C will be considered.

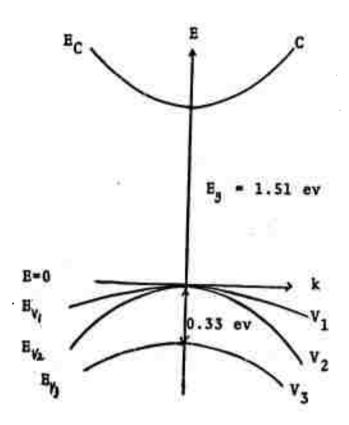


Figure 2-1-1. GaAs Band Structure (10)

```
C: Conduction band V_1: heavy hole band V_2: high hole band V_3: split-off band V_3: split-off band V_3: electron rest mass V_4: effective mass in band V_4: V_4: V_4: effective mass in band V_4: V_4: V_4: the energy of electron in the V_4 band where V_4: V_4
```

Transition probability W via two photon absorption can be calculated using second order perturbation theory. Let total transition probability be  $W = W_1 + W_2$  where  $W_i$  is individual transition probability from ith valence band to conduction band. We need to calculate  $W_i$  for i = 1, 2.

$$W_{i} = \frac{2\pi}{\pi} \int \int d^{3}k_{f} d^{3}k_{i} \left( \sum_{\nu} \frac{\langle i | H' | \nu \rangle \langle \nu | H' | f \rangle}{E_{\nu} - E_{i} - \hbar \omega} \right)^{2}$$

$$\times \delta(E_f - E_i - 2\hbar\omega)$$
 (2-1-2)

where  $H' = \frac{e}{mc} \vec{P} \cdot \vec{A}$ ; perturbing Hamiltonian

- |i> denotes initial state
- If denotes final state
- |V> denotes intermediate state
- πω; single photon energy of incident radiation

The initial state is one of the valence bands and the final state is the conduction band. There are two photons which participate simultaneously in this process. The two photon absorption process can be considered as follows. An electron is excited from an initial state i (valence band) to a final state f (conduction band) through a virtual intermediate state v by absorbing two photons. Basov (1) considered both the conduction band and the valence band as intermediate states. If we take one intermediate state as conduction band (the final state) and the other as a valence band (the initial state), and neglect the contribution from other intermediate states, then W, becomes as follows.

$$W_{i} = \frac{2\pi}{\hbar} \iiint d^{3}k_{c} d^{3}k_{V_{i}} \left( \frac{H_{V_{i}c} H_{cc}}{E_{c} - E_{V_{i}} - \hbar\omega} + \frac{H_{V_{i}V_{i}} H_{V_{i}c}}{E_{V_{i}} - E_{V_{i}} - \hbar\omega} \right)^{2}$$

$$\times \delta(E_{c} - E_{V_{i}} - 2\hbar\omega) \qquad (2-1-3)$$

where  $H'_{CC} = \langle \psi_C | H' | \psi_C \rangle$   $H'_{CV_i} = \langle \psi_C | H' | \psi_{V_i} \rangle$ ... etc.  $H'_{CV_i} = (H'_{V_iC})^{\dagger}$ 

 $^{\psi}$ c,  $^{\psi}$ V<sub>i</sub> are wave function in band C and V<sub>i</sub>

Two photons can be absorbed only when  $E_c$  -  $E_{V_i}$  =  $2\hbar\omega$ . Thus

$$W_{i} = \frac{2\pi}{\hbar} \frac{1}{(\hbar\omega)^{2}} \iint d^{3}k_{c} d^{3}k_{V_{i}} \left( H_{cc} H_{cV_{i}} + H_{cV_{i}} H_{V_{i}V_{i}}^{\prime} \right)^{2}$$

$$\times \delta(E_{c} - E_{i} - 2\hbar\omega) \qquad (2-1-4)$$

In order to derive matrix elements, we have to know the wave functions. The wave function of the electrons in the respective bands can be written as the normalized Bloch functions.

$$\psi_{c}(\overline{k}) = \frac{1}{(2\pi)^{3/2}} U_{c}(\overline{r}) \exp(i\overline{k}_{c} \cdot \overline{r})$$

$$\psi_{V_{i}}(\overline{k}_{V_{i}}) = \frac{1}{(2\pi)^{3/2}} U_{V_{i}}(\overline{r}) \exp(i\overline{k}_{V_{i}} \cdot \overline{r})$$
(2-1-5)

where  $\psi_c$  and  $\psi_{V_i}$  are normalized, and  $U_c(\overline{r})$  and  $U_{V_i}(\overline{r})$  are functions of the position vector  $\overline{r}$  over the dimensions of a unit cell.

Thus

$$H_{cV_{i}} = \frac{e}{mc} \langle \psi_{c}(\overline{k}_{c}) | \hat{P} \cdot \overline{A} | \psi_{V_{i}}(\overline{k}_{V_{i}}) \rangle$$

$$= \frac{eA}{mc} (\hat{P} \cdot \overline{\alpha})_{cV_{i}} \delta(\overline{k}_{c} - \overline{k}_{V_{i}}) \qquad (2-1-6)$$

where 
$$(\hat{P} \cdot \vec{\alpha})_{cV_i} = \langle U_c(\vec{r}) | \hat{P} \cdot \vec{\alpha} | U_{V_i}(\vec{r}) \rangle$$

Note that photon wave vector is small compared with crystal momentum  $k_c$  or  $k_{V_i}$ . Thus  $\delta(\overline{k}_c - \overline{k}_{V_i})$  implies a vertical transition since  $H_{cV_i}$  is not zero only when  $\overline{k}_c = \overline{k}_{V_i}$ .

Note that

$$\widehat{\beta} \mid \psi \rangle = \frac{m}{\pi} \frac{\partial E}{\partial k} \mid \psi \rangle \tag{2-1-7}$$

where P is the operator of momentum P.

Let  $\overline{X} = A\overline{\alpha}$ 

where  $\overline{\alpha}$  is the polarization vector.

Using the relation (2-1-7), we can easily get

$$H_{CC} = \frac{eA}{m_c * C} (\hbar k_c \alpha) \delta(\overline{k}_c - \overline{k}_c') \qquad (2-1-8)$$

$$H_{V_{i}V_{i}} = \frac{-eA}{m_{V_{i}}*c} (\hbar k_{V_{i}} \alpha) \delta(\bar{k}_{V_{i}} - \bar{k}_{V_{i}}')$$
 (2-1-9)

where m<sub>c</sub>\* and m<sub>V</sub>\* are the effective masses of the electron in the conduction band and the hole in the valence band.

Substituting these values in equation (2-1-4) we get  $W_i$  (see Appendix I).

$$W_{i} = \frac{2^{\frac{17}{2}} \pi e^{4}}{\varepsilon c^{2} (\hbar \omega)^{6}} \frac{\left| (\bar{\alpha} \cdot \hat{P})_{cV_{i}} \right|^{2}}{m^{2}} m_{cV_{i}}^{*} (2\hbar \omega - E_{g})^{3/2} I^{2}$$
 (2-1-10)

where m: free electron mass

$$m_{cV_{i}}^{*} = \frac{m_{c}^{*} m_{V_{i}^{*}}}{m_{c}^{*+m_{V_{i}^{*}}}}$$

ε; dielectric constant

Eg; Energy gap

and I is the intensity of radiation in the medium

$$I = v N \hbar \omega = \frac{v \varepsilon E^2}{8\pi} = \frac{v \omega^2 \varepsilon A^2}{8\pi c^2}$$

Since 
$$\overline{E} = -\frac{1}{c} \frac{\partial \overline{A}}{\partial t}$$

$$A \sim e^{i\omega t}$$

$$E = \frac{\omega}{c} A$$

$$A = |\overline{A}|$$

$$E = |\overline{E}|$$

Note that 
$$v = \frac{c}{\epsilon^{1/2}}$$

N = photon density

**E** = electric field intensity

 $\overline{A}$  = the vector potential

Thus the transition probability per unit volume W, is

$$W_{i} = \frac{W_{i}}{V} \frac{2^{\frac{17}{2}} \pi e^{4}}{\varepsilon c^{2} (\hbar \omega)^{6}} \frac{|(\hat{P} \cdot \bar{\alpha})_{cV_{i}}|^{2}}{m^{2}} m_{cV_{i}}^{*1/2} (2\hbar \omega - E_{g})^{3/2} I^{2}$$

$$W = W_{1} + W_{2} = \partial_{i} I^{2} \qquad (2-1-11)$$

Absorption coefficient  $K_i$  is defined as follows

$$K_{i} = -\frac{1}{I} \frac{dI}{dX} = \frac{2\hbar \omega W_{i}}{I}$$

where X is the penetration depth of radiation from the surface of the crystal

$$K_{i} = \frac{2^{\frac{19}{2}\pi e^{4}}}{\varepsilon c^{2}(\hbar\omega)^{5}} \frac{|(\hat{P} \cdot \bar{\alpha})_{cV_{i}}|^{2}}{m^{2}} m_{cV_{i}}^{*}^{1/2} (2\hbar\omega - E_{3})^{3/2} I$$

Total two photon absorption coefficient is sum of  $K_1$ 's for i = 1,2.

$$\mathbf{K}^{(2)} = \mathbf{K}_1 + \mathbf{K}_2$$

The calculation of K of GaAs is shown in Appendix II.

The intensity dependence on the depth of penetration into the crystal can be calculated from the following equation.

$$\frac{dI}{dX} = -2\hbar\omega W - KI = -\beta I^2 - KI$$
 (2-1-12)

where  $W = W_1 + W_2$ 

X: depth of penetration

K: two photon absorption coefficient

K: one photon absorption coefficient

 $W = \alpha I^2$ ,  $\beta = 2\hbar\omega a = K^2/I$ 

If we solve the equation (2-1-12) (see Appendix III),

$$I = \frac{I_0 \exp (-KX)}{1 + \frac{\beta I_0}{K} [1 - \exp(-KX)]}$$

where  $I_0$  is initial intensity of exciting radiation. This expression can be approximated as

$$I(X) = \frac{I_0}{\beta X I_0 + 1}$$
 (2-1-13)

if KX << 1 .

This is the case when two photon absorption is dominant.

If the absorption is mostly due to a one photon process,

$$I(X) = I_0 e^{-KX}$$
 (2-1-14)

These calculations can be applied to Nd:glass laser pulse as exciting source.

## 52. The Spectral Linewidth Narrowing

As we will see from the experimental results, the spectral width above the threshold becomes very narrow but finite. Even though the power level of the exciting heam is below the threshold, the spectral width becomes narrower as the power increases. This spectral width narrowing occurs in the emission spectrum from the crystal even without resonant mirrors. This can be explained in terms of the superradiance.

## a. The Spectral Width of the Laser Output

The finite spectral width of the output of a laser oscillator is due to the presence of random phase and amplitude fluctuations in its output field. These random fluctuations are caused by the radiative spontaneous transitions from the upper laser level.

A laser oscillator can be considered as a regenerative amplifier with a continuous input of spontaneous emission noise. Thus by using the laser equivalent circuit, the expression for the spectral width of the laser output was derived by Gordon (11), Schawlow and Townes (12). The result, taking into account only amplitude fluctuations, is as follows.

$$\Delta v = \frac{2\pi h \, v_0 \, (\Delta v_c)^2}{p} \, \frac{N_2}{\left[N_2 - N_1 \, \frac{g_2}{g_1}\right]_{th}}$$
 (2-2-1)

where  $\Delta v$ : the spectral width of the laser output

va: resonant frequency

 $\Delta v_c$ : the width of passive cavity response curve or cavity bandwidth

P: the total power leaving the cavity

 $N_1$ : the population density of the lower level

N<sub>2</sub>: the population density of the upper level

g1,g2: the level degeneracies

$$\left[N_2 - N_1 \frac{g_2}{g_1}\right]_{th}$$
: the value of the threshold

As we shall see, the foregoing arguments justify the finite linewidth observed in the laser emission spectrum.

b. The Spectral Width Narrowing Below the Threshold This type of narrowing is known as the super-radiant narrowing in fluorescence radiation. The spontaneous recombination radiation emitted with a lineshape g(v) is amplified in passing through the medium by a factor  $e^{ag(v)}$  where a is a constant which is proportional to the degree of inversion. A Yariv (13) studied the superradiance. The gain constant  $\gamma(v)$  is given as follows.

$$\gamma(v) = ag(v) = \frac{c^2 \left(N_2 - N_1 \frac{g_2}{g_1}\right)g(v)}{8\pi v^2 \text{ t spont}}$$
 (2-2-2)

where  $\gamma(\nu)$ : the gain of the optical system

c : the velocity of light

 $N_1, N_2, g_1, g_2$ ; same as in the previous section

g(v): the line shape of spontaneous recombination radiation.

Thus the intensity of the radiation at the position  $\chi$  from the surface is

$$I(X) = I_0 e^{\gamma(\nu)\chi} = I_0 e^{ag(\nu)\chi}$$
 (2-2-3)

where  $I_0 = I(0)$ 

But since the line shape narrows as the light propagates,  $g(\nu)$  actually depends also on  $\chi$ . Thus we have to modify above equation.

$$I(X) = I_0 e^{a \int_0^X g(X,v)dX} = I_0 e^{aF(v)}$$
 (2-2-4)

where  $F(v) = \int_{0}^{X} g(X,v)dX$ 

Yarrvet al. showed that the line shape of the spontaneous emission is

$$F(v) = g(v) \frac{e^{\left[\gamma(v) - \alpha\right]\ell} - 1}{\gamma(v) - \alpha}$$
 (2-2-5)

where a: a distributed loss constant

1: the length of crystal

vo: the frequency at which the line maximum occurs.

An immediate consequence of the equation (2-2-5) is that for  $\gamma(\nu_0)$ ? << 1,  $F(\nu)$  = const  $g(\nu)$  and no change in the spectrum is expected. The more interesting condition is that if  $\gamma(\nu_0)$ ? >> 1 but  $\alpha$  >>  $\gamma(\nu_0)$ , no narrowing occurs since  $F(\nu)$  = const  $g(\nu)$ . If  $\gamma(\nu_0)$  is increased to a point where it becomes comparable yet smaller than  $\alpha$ ,

$$F(v) = const \left\{ \frac{g(v)}{\gamma(v) - \alpha} \right\}$$

which is, because of the frequency-dependent denominator, narrower than g(v).

It is clear from the above that spectral narrowing, unlike laser action, is a gradual process and no exact narrowing condition can be given. At the same time we can summarize the observations made in previous part by giving the following approximate condition for "starting" of narrowing

$$\gamma(v_0) = 1$$

$$\gamma(v_0) = \alpha$$
(2-2-6)

The physical interpretation of this result is as follows. Condition (2-2-6) is equivalent to say that a photon emitted at  $\nu_0$ , on the average, stimulates the emission of

order of 1 photon in a distance 2. Photon emitted at the wings of g(v) have, according to equation (2-2-4), a much smaller probability of inducing emissions so that the condition (2-2-6) marks the point at which the photon distribution is beginning to vary appreciably from g(v). If we limit ourselves to cases where

$$\gamma(\nu_0) \ell >> 1 
\gamma(\nu_0) > \alpha$$
(2-2-7)

and define  $\Delta_{\nu}$  as the width at half-maximum of  $F(\nu)$  and  $(\Delta\nu)_g$  as the width at half-maximum of  $g(\nu)$ , Gordon derived the amount of narrowing  $\Delta\nu/(\Delta\nu)_g$  at a given value of  $\gamma(\nu_0)$ . The result is

$$\frac{\Delta v}{(\Delta v)_g} = [\gamma(v_0)l] \quad \text{for a Gaussian } g(v) \qquad (2-2-8)$$

$$\frac{\Delta v}{(\Delta v)_g} = 0.832 \left[ \gamma(v_0) \ell \right]^{-1/2} \text{ for a Lorentzian } g(v) (2-2-9)$$

53. The Threshold Pumping Power for Oscillation and Lasing First let's discuss about the oscillation condition.
The rate equation for the electrons in conduction band is as follows.

$$\frac{dn_c}{dt} = W - \frac{n_c}{\tau_S}$$
 (2-3-1)

where

n; electron concentration in conduction band

W; transition probability

 $\tau_S$ ; spontaneous lifetime of electron

The rate of increase of electrons in conduction band is the difference between stimulated upward transition and downward transition due to spontaneous emission. The threshold condition can be determined by letting

$$\frac{dn_c}{dt} = 0$$

Then

$$W = \frac{n_c}{\tau_S}$$
 (2-3-2)

As we derived before W is a function of  $I^2$ . Let W =  $aI^2$ . Thus

$$aI_{oS}^2 = \frac{n_c}{\tau_S}$$
 where  $I_{oS}$  denotes threshold pumping power density for oscillation

This is the threshold for stimulated emission, not for laser action.

$$I_{OS} = \sqrt{\frac{n_c}{a\tau_S}}$$
 (2-3-3)

This is the threshold pumping power density for oscillation. But the threshold for lasing would be higher than this due to the losses. The losses are the sum of reflection losses at the mirrors of the optical cavity and the diffraction losses. Let  $K_{loss}$  be the losses. If  $\alpha$  is the gain in the laser medium, at the threshold for lasing, then the following relation is satisfied.

$$\sqrt{R_1 R_2} e^{(\alpha - K_{loss})L} = 1$$
 (2-3-4)

where R<sub>1</sub>,R<sub>2</sub>: the reflection coefficient of the resonator mirrors,

L ; effective optical length of cavity,

K<sub>loss</sub>; loss

a ; gain

The gain is the function of pumping power density I. This is given in the Basov's paper (1). Then from (2-3-4)

$$\alpha(I) = \frac{1}{2L} \ln R_1 R_2 + K_{loss}$$
 (2-3-5)

$$\alpha(I) = K^{(i)} \frac{1}{4kT} (\mu - \hbar \omega_g) \left[ 1 + \frac{K^{(i)}I}{4kTB\hbar \omega_g} \right]^{-1}$$
 (2-3-6)

where  $K^{(i)}$ ; absorption coefficient where i = 1,2

 $\mu$ : Fermi quasi level of the electrons ( $\mu_e$ )

and the holes  $(\mu_n)$ 

 $\omega_{\mathbf{g}}$ : generation frequency

B : the derivative of recombination rate with respect to the sum of quasi levels  $\mu$  at

the point corresponding to the oscillation

threshold  $\mu_{OS}$ .

T : carrier temperature

k : Boltzman const.

From (2-3-5) and (2-3-6), the threshold pumping power density  $I_{OS}$  for lasing can be derived.

#### CHAPTER III

#### **EXPERIMENT**

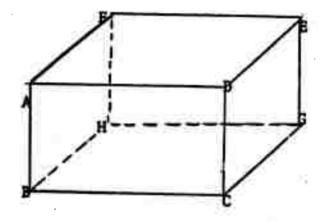
First, the emission spectra of GaAs were observed at different levels of pump power density. Secondly, the dependence of output power from the GaAs crystal was studied. To carry out these experiments the power calibration of the photodiode was required. The arrangement of the pumping laser system was important but it is described elsewhere. (See Appendix IV.)

In this chapter mainly describes the design of the experiments. The results are discussed in the next chapter.

## \$1. The Spectral Emission Lines from GaAs

to get spontaneous and stimulated recombination radiation. The Nd:glass laser was used as the pump. The maximum power density was approximately 50 MW per unit area (cm<sup>2</sup>) at the front surface of the GaAs crystal. The description of exciting pulse is shown in §4 of this chapter.

The GaAs crystal with dimensions of 4 mm x 5 mm x 10 mm, has a carrier concentration, i.e., impurity density, of about  $2 \times 10^{17}/\text{cm}^3$ . The mobility of the crystal is approximately  $4000 \text{ cm}^2/\text{v-sec}$  at room temperature.



AD = 10 mm

EG = 4 mm

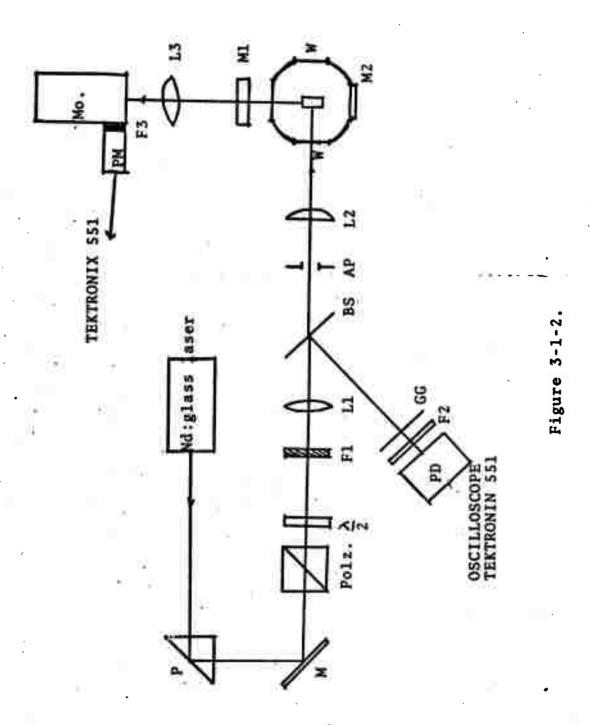
CG = 5 mm

Figure 3-1-1. Dimension of the GaAs Crystal

The Figure 3-1-1 is given for convenience to identify directions of surfaces which will be referred later.

The bulk crystal was prepared such that the surfaces of bulk coincided with the specific planes of GaAs crystalline structure. GaAs has the cubic zinc sulfide structure. The positions of the Ga atoms in the unit cell are at 0.00; 0.12, 1.22; 1.22, 0.12; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22, 0.22; 1.22; 1.22, 0.22; 1.22

orientation of the plane ( hkl) is expressed in Miller Optical polishing was done on all faces, with particular emphasis on the two 4mm x 5mm end faces. Broad band anti-reflection coating was done on two 4mm x 5mm end faces and on one of the (1 1 0) faces (i.e., MABCD face shown in the Figure 3-1-1; the wavelength ranges from 8200 Å to 1.1  $\mu$  for reflectivity less than 1%). The face ABCD was placed perpendicular to the exciting neodymiumglass laser beam. The crystal was attached to a cold finger placed in liquid nitrogen (77°K). The diagram of dewar which contained the cold finger and crystal in vacuum is shown in Appendix VI. The direction of the Nd: glass laser beam was changed by 180° using a prism and a mirror mounted on a venier. This was done because was another experiment required the same Nd: glass laser. The prism (P) could be moved in and out of the path of the Nd: glass laser beam. All these arrangements are shown in Figure 3-1-2 in block dia-The polarizer was used to be sure that the beam was gram. polarized in one direction. In this case it was horizontally polarized. The half wave plate was used for changing the polarization to the vertical direction. Calibrated neutral density filters were used to vary the pump intensity incident on the crystal. The diameter of the spot of the beam was larger than the width of the crystal surface on which exciting radiation was incident. We also used a set



## NOTATIONS in Figure 3-1-2

P : Prism

M : Mirror

Polz: Polarizer

 $\frac{\lambda}{3}$ : Half wave plate

F1: Neutral density filter

F2: Neutral density filter

F3: Filter for filtering flash light (No. 2-58 Corning

glass color filter)

L1 : Lens

L2 : Cylindrical lens

AP : Aperture

M1 : Mirror

M2 : Mirror

D ': Dewer

S : Sample

w : Window

Mo: Monochromator (Jarrel Ash 82-020)

PM : Photomultiplier (RCA 7102)

PD: Photodiode (RCA 917)

of lenses L1 and L2. As the crystal was shorter in height than in lengh, i.e., AB ( AD, we used the cylindrical lens (L2) to narrow beam spot along the AB direction. The aperture (AP) was used as the reference point to check correctness of the direction of exciting As the Nd:glass laser pulses were not always of same power level even for the same operating conditions, i.e., for the same dye concentration and the same operating voltage, it was necessary to monitor the exciting laser pulse. If we a put beam splitter (BS) after lens (L1), then part of the enters photodiode (PD) through the ground glass (GG) and neutral density filter (F2). The ground glass and neutral density filter prevent saturation of the photodiode. The details of the photodiode circuit diagram is presented in Appendix V. The GaAs crystal was attached to the cold finger in the dewar (D) which was evacuated by the air pumping. The cold finger was mounted on the container in which we supplied liquid nitrogen. crystal and cold finger remained at liquid nitrogen temperature, 77°K. There were three windows on the cylindrical wall of dewar. In one side of the crystal one mirror (M2) which had 99% reflectivity was placed. The other mirror (M1) was mounted on a vernier mounc. These M1 and M2 constitute the laser cavity. The generated radiation from the GaAs laser was focused by the lens (L3) and sent into the entrance slit of the monochromator.

The signals from the photodiode (PD) and from the photomultiplier (PM) were connected to the upper and the lower
input terminals of a dual beam oscilloscope, respectively.

As we will see in next section, we can calibrate the photodiode such that the peak value of the pulse in the photographs corresponds to the power of the laser pulse. For
a fixed power level, we took photographs of the exciting
and emitted radiation pulses as we varied the wavelength
dial of the monochromator. Figure 4-1-1 shows the emission
spectrum of GaAs crystal.

§2. The Dependence of the Power Density Radiated by GaAs upon the Exciting Light Intensity

It was necessary to calibrate the photodiode . . in order to relate the power and the peak value of the pulse photographed from the oscilloscope.

The arrangement of the experimental equipment and the result of the experiment will be presented later.

First, the output power dependence will be discussed.

The experimental setup is the same as in previous experiment.

Here we fixed the wavelength dial of the monochromator at the value corresponding to peak value in emission spectrum, i.e., 8386 Å. Then we introduced neutral density filters in F1 in Figure 3-1-2. The exciting pulse was monitored using the photodiode (PD) and sent to upper trace terminal

of the Tektronix 551 oscilloscope; the radiation from the GaAs crystal was collected through monochromator, amplified by photomultiplier (PM) and sent to lower trace terminal of the oscilloscope. The two signals were then simultaneously photographed. The result of this experiment after analyzing the data is given in Chapter IV.

#### 53. The Power Calibration of the Photodiode

In this experiment the power of the emission spectrum had to be estimated because we had to find the power level where the narrowing of the width in emission spectrum occurred. In the second experiment it was more necessary because we had to know the power or intensity of the exciting beam. Figure 2-1-5 shows the arrangement of experimental equipment for calibration of photodiode. The neutral density filters (F1) and (F), the lens (L1), beam splitter (BS) and ground glass (GG) where used for same reasons which were discussed previously. The lens (L2) was used to focus the beam into the hole of the thermopile. The thermopile was calibrated as following.

[ $\mu V$  reading/198.2] = The energy [joules]

If we can measure the pulse width, then we can calculate power as follows.

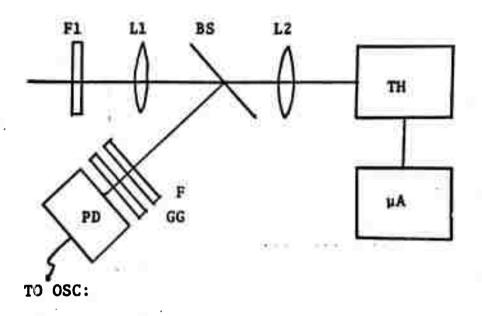


Figure 3-3-1.

F1: Neutral density filter

L1: lens

L2: lens

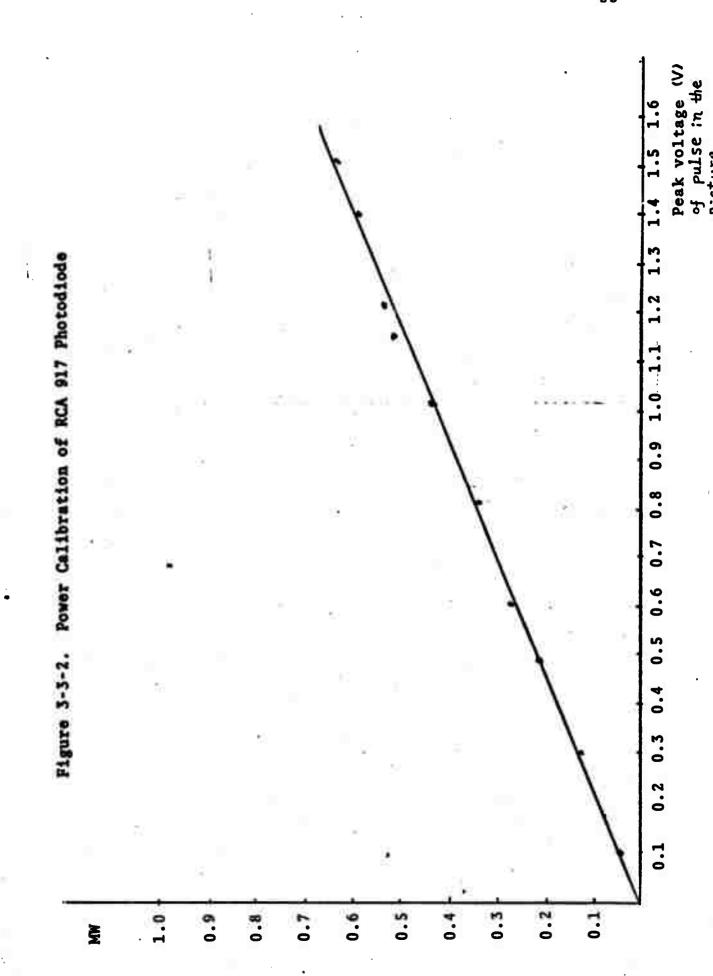
BS: beam splitter

F: ND 2.0 neutral density filter

GG: Ground glass

TH: TRG 100 thermopile

μA: Microammeter



Power in MW = 
$$\frac{\mu V}{198.2} \times \frac{10^9}{W} \times \frac{1}{10^6}$$

where μV; microvoltmeter reading in [μV]

W; width of the pulse in [n sec] .

If we divide power by the area of the spot of the beam on the surface of the sample, we can calculate power density I.

where MW is power in [MW]

S is area of beam spot in  $[cm^2]$ I is power density in  $\left[\frac{MW}{cm^2}\right]$ 

Figure 3-3-2 shows the power vs. peak of the pulse which was taken on the photograph.

## **\$4.** The Pumping Source

As we mentioned before, Nd:glass laser was used as the pumping source. The Nd:glass laser rod was of dimensions, 0.5" diameter and 8.31" length. The ends of the rod were cut at Brewster angles to avoid reflection losses. The rod was placed inside an open resonator consisting of two mirrors (99.9% reflectivity and 65% reflectivity at  $1.06~\mu$ ). The Nd:glass laser was Q-switched with a dye

cell inside the cavity. Eastman Kodak dye solution (No. 9860) was used. The Q-switched pulse had a maximum power of about 50 MW/cm<sup>2</sup> with a pulse width of about 150 n sec. To insure that only the Q-switched nanosecond pulse was generated we inserted a mode selector inside the laser cavity to prevent mode-locking.

#### CHAPTER IV

#### THE EXPERIMENTAL RESULTS AND DISCUSSION

#### \$1. The Emission Spectrum from GaAs

Figure 4-1-1 shows the emission spectrum of GaAs crystal. The ratio of output power density of the emitted radiation with respect to the power density of exciting beam was plotted on the y-axis and the wavelength of emission spectrum on the x-axis. The curve 1 in Figure 4-1-1 is the emission spectrum at the exciting power density, approximately 2MW/cm<sup>2</sup>. The curve 2 is that at 5MW/cm<sup>2</sup>. The curve 3 is that at 10MW/cm<sup>2</sup>. We increased the level of exciting power density by reducing the value of the neutral density filter (F1). In Figure 4-1-1, we can see that the width of the emission spectrum of curve 1 was about 390 A and it was narrowed to about 200 A at curve 2 and-then it was narrowed abruptly down to 16 A. We expected these narrowings of the widths of the emission spectrums as discussed in Chapter II. We saw that there were mainly two different reasons for narrowing of the width of the emission spectrum.

First, let's discuss about the linewidth narrowing due to the laser action. The linewidth of the emission spectrum in curve 2 was about 200 Å. It was narrowed abruptly to about 16 Å in curve 3. This indicates there occurs laser action. But because of the limited resolution of the

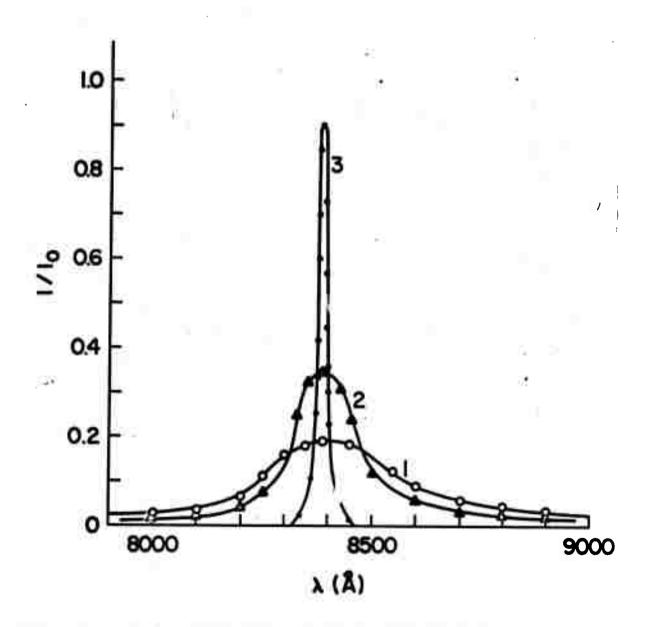


FIG 4-1-1 THE VERTICAL SCALE OF CURVE 1,2 IS MAGNIFIED 8 TIMES.

monochromator, it was hard to detect a spectral line marrover than the order of 10 Å. Next note that the width of 390 Å of curve 1 narrowed to 200 Å of curve 2.

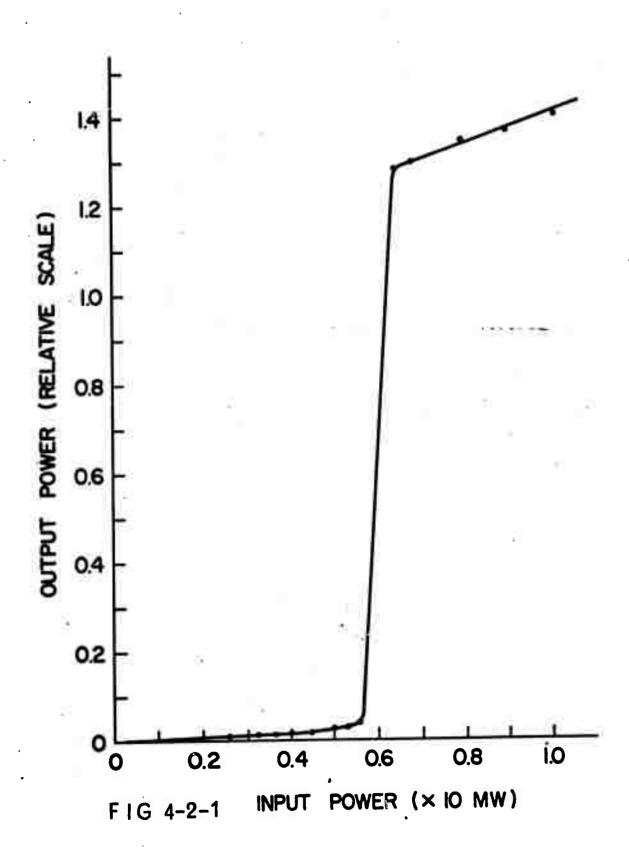
The power density of exciting beam was about  $5 \text{ MW/cm}^2$  for curve 2. As we can see in next section it was below the threshold. This is the narrowing due to the superradiance. If we increase the power density of the exciting beam then according to the equation (2-2-2),  $\gamma(\nu_0)$  increases. Then in equation (2-2-8)

$$\frac{\Delta v}{(\Delta v)_g} = [\gamma(v_0) \ell]^{-1/2},$$

we can see  $\Delta \nu$  decreases as  $\gamma(\nu_0)$  l increases. This justifies the line narrowing below threshold.

§2. The Dependence of Power Density of Radiation from GaAs on the Exciting Light Intensity

Using the data we got in the experiment of §2, Chapter III, we can draw a graph shown in Figure 4-2-1. As the photodiode was calibrated in Figure 3-3-2, we can find absolute power density of exciting signal. Figure 4-2-1 shows the graph in x-axis correspond to the intensity of the exciting beam and y-axis correspond to the output . power in arbitrary scale. It can be easily seen that at 5-6 (MW/cm<sup>2</sup>) power level the power of emitted radiation



jumps up to a higher level. So we can say this value correspond to the threshold for lasing. Of course, this data was taken by varying the value of the neutral density filter. It was better to start at a low power level, because at high power levels the surface of the crystal may be damaged. According to the experiment approximately 50 MW/cm<sup>2</sup> was the maximum intensity tolerated by the crystal. If the power density of incident beam is higher than this, it might give damage on the surface of the sample. According to the Figure 4-2-1 it is obvious that the part of the graph threshold is due to spontaneous emission, and the part of the graph above threshold is because of the stimulated emission. The output power when the GeAs is lasing, is 30~50 times that of the fluorescence below the threshold. In the threshold region, the ratio is around 30.

The threshold power density for oscillation can be calculated using the equation (2-3-3)

$$I_{OS} = \sqrt{\frac{n_c}{a\tau_S}}$$

The threshold concentration of electrons in the conduction band can be calculated using the population inversion condition.

The iteration method is presented in C. Chang's (8)

paper. Dumke (7) calculated the radiative lifetime of an electron in the conduction band of semiconductor GaAs. Here

it is only necessary to estimate the level of threshold intensity

According to above papers,

$$n_c \sim 10^{19} \text{ electrons/cm}^3$$
 $\tau_c \sim 10^{-7} \text{ sec}$ 

From appendix II  $a=0.15 \left[ \frac{\text{cm} \cdot \text{sec}}{\text{erg}^2} \right]$ 

Since  $aI_{OS}^2 = 10^2$  and we want  $I_{OS} \text{ in } \left[ \frac{\text{MW}}{\text{cm}^2} \right]$ ,

 $0.15 I_{OS}^2 \times (10^7)^2 \times (10^6)^2 = 10^{26}$ 
 $I_{OS}^2 \sim 6.7$ 
 $I_{OS} \sim 2.6 \text{ [MW/cm}^2]$ 

This is the threshold pumping power density for oscillation. The threshold for lasing would be higher than this. The experimental value was about 5 MW/sec. If we recall that approximate values of electron density and spontaneous lifetime were used, and if we admit experimental deviation, the order of the experimental result can be considered good enough.

#### APPENDIX I

## DERIVATION OF Wi

$$W_{i} = \frac{2\pi}{\hbar} \left(\frac{1}{\hbar\omega}\right)^{2} \int \int d^{3}k_{c} d^{3}k_{V_{i}} \left(H_{cc} H_{cV_{i}} + H_{cV_{i}} H_{V_{i}V_{i}}\right)^{2}$$

$$X \delta(E_{c} - E_{V_{i}} - 2\hbar\omega)$$
 (1)

$$H_{cV_{i}} = \frac{eA}{m_{c}^{*}c} (\overline{P} \cdot \overline{\alpha})_{cV_{i}} \delta(\overline{k}_{c} - \overline{k}_{V_{i}}) \qquad (2)$$

$$H_{CC}^{\prime} = \frac{eA}{m_{C}^{*}} (\hbar k_{C} \alpha) \delta(\overline{k}_{C} - \overline{k}_{C}^{\prime})$$
(3)

$${}^{H}\widetilde{\mathbf{v}}_{\mathbf{i}}\mathbf{v}_{\mathbf{i}} = \frac{-eA}{{}^{m}\mathbf{v}_{\mathbf{i}}\mathbf{c}} \left(h \ k_{\mathbf{v}_{\mathbf{i}}} \ \alpha\right) \ \delta(\overline{\mathbf{k}}_{\mathbf{v}_{\mathbf{i}}} - \overline{\mathbf{k}}_{\mathbf{v}_{\mathbf{i}}}') \tag{4}$$

Substitute equations (2), (3) and (4) in (1). Note that

$$\int \psi_c^* \psi_{V_i} d^3 r = \delta(\bar{k}_c - \bar{k}_{V_i})$$

$$\frac{v}{(2\pi)^3} \int U_c^* U_{V_i} d^3r = \langle U_c | U_{V_i^*} = \delta_{cV_i}$$

$$\delta^2(\overline{k}) = (2\pi)^{-3} V \delta(\overline{k})$$

After operating  $\delta$  functions,

$$\bar{\mathbf{k}}_{\mathbf{c}} = \bar{\mathbf{k}}_{\mathbf{V}_{\mathbf{i}}}$$

so let 
$$\bar{k}_c = \bar{k}_{V_i} = \bar{k}$$

Then

$$W_{i} = \frac{W_{i}}{V} = \frac{2\pi}{\hbar} \left(\frac{1}{2\pi}\right)^{3} \left(\frac{1}{\hbar\omega}\right)^{2} \frac{e^{4}A^{4}}{m^{2}c^{4}} h^{2} \alpha^{2} |(\overline{P} \cdot \overline{\alpha})_{cV_{i}}|^{2} \left(\frac{1}{m_{c}^{*}} + \frac{1}{m_{V_{i}}^{*}}\right)$$

$$\times \int d^{3}k k^{2} \delta(E_{c} - E_{V_{i}} - 2\hbar\omega)$$

Let 
$$m_{cV_{i}}^{*} = \frac{m_{c}^{*} m_{V_{i}}^{*}}{m_{c}^{*} + m_{V_{i}}^{*}}$$

Note that

$$E_{c} - E_{V_{i}} = E_{g} + \left(\frac{h^{2} k_{c}^{2}}{2m_{c}^{*}} + \frac{h^{2} k_{V_{i}}^{2}}{2m_{V_{i}}^{*}}\right)$$

$$= \frac{\hbar^{2} k^{2}}{2m_{c}V_{i}} + E_{g}$$

$$\delta(f(X)) = \frac{d(X-X_0)}{\left|\frac{df(X)}{dX}\right|} \quad \text{where } f(X_0) = 0$$

$$\frac{d(E_{c} - E_{V_{i}} - 2\hbar\omega) = \delta\left(\frac{h^{2} k^{2}}{2m_{c}V_{i}} + E_{g}\right)}{\frac{\delta(k-k')}{\frac{\hbar^{2} k'}{m_{c}V_{i}}} = \frac{m_{c}V_{i}}{h^{2} k'} \delta(k-k')}$$

Let

$$I = \int d^{3}k k^{2} \delta(E_{c} - E_{V_{i}} - 2\hbar\omega)$$

$$I = \int d^{3}k k^{2} \frac{^{m}cV_{i}}{^{n}^{2}k'} (k-k')$$

$$= \int d^{3}k' k' \frac{^{m}cV_{i}}{^{n}^{2}}$$

$$= \frac{^{m}cV_{i}}{^{n}^{2}} \int k' d^{3}k'$$

Since 
$$d^3k' = 4\pi k^{-2}dk'$$

$$I = \frac{m_{cV_{i}}^{*} 4\pi}{\hbar^{2}} \int dk' k'^{3} \delta(k-k')$$

$$= \frac{m_{cV_{i}}^{*}}{\hbar^{2}} 4\pi k^{3}$$

$$\frac{\hbar^2 k^2}{2m_{cV_i}} + E_g = E_c - E_{V_i} = 2\hbar\omega$$

$$k^2 = \frac{2m_{cV_i}}{\pi^2} (2\hbar\omega - E_g)$$

$$k^{3} = \frac{2^{\frac{3}{2}} m_{cV_{1}}^{\frac{3}{2}} (2\hbar\omega - E_{g})^{\frac{3}{2}}}{\pi^{3}}$$

$$I = \frac{2^{\frac{7}{2}} \pi^{m_{c}} V_{i}^{\frac{5}{2}}}{\pi^{5}} (2\hbar\omega - E_{g})^{\frac{3}{2}}$$

$$W_{i} = \frac{2\pi}{\hbar} \left(\frac{1}{2\pi}\right)^{3} \left(\frac{1}{\hbar\omega}\right)^{2} \frac{e^{4}A^{4}}{m^{2}c^{4}} h^{2} \alpha^{2} |(\overline{P} \cdot \overline{\alpha})_{cV_{i}}|^{2} \frac{1}{m_{cV_{i}}^{*}}$$

$$\times \frac{2^{\frac{7}{2}} \pi m_{cV_{i}}^{*}}{\hbar^{5}} (2\hbar\omega - E_{g})^{\frac{3}{2}}$$

The intensity of radiation in the medium

$$I = \sqrt{N}\hbar\omega = \sqrt{\varepsilon} \frac{E^2}{8\pi} = \frac{\sqrt{\omega^2 \varepsilon A^2}}{8\pi c^2}$$

since 
$$\overline{E} = -\frac{1}{c} \frac{\partial \overline{A}}{\partial t}$$

$$A \sim e^{i\omega t}$$

$$E = \frac{\omega}{c} A$$

If we take account spin degeneracy, and  $\alpha^2 = 1$ ,

$$W_{i} = \frac{2^{\frac{17}{2}} \pi e^{4}}{\varepsilon c^{2} (\hbar \omega)^{6}} \frac{|(\hat{P} \cdot \overline{\alpha})_{cV_{i}}|^{2}}{m^{2}} m_{cV_{i}}^{*\frac{1}{2}} (2\hbar \omega - E_{g})^{\frac{3}{2}} I^{2}$$

#### APPENDIX II

## CALCULATION OF TWO PHOTON ABSORPTION COEFFICIENT

$$W = aI^2 \qquad \left[ \frac{1}{\sec \cdot ch.^2} \right]$$

where

$$a = \sum_{i=1,2}^{1} \frac{\frac{17}{2^2} \pi e^4}{\epsilon c^2 (\hbar \omega)^6} (2\hbar \omega - E_g)^{\frac{3}{2}} \frac{|(P \cdot \overline{\alpha})_{cV_i}|}{m} m_{cV_i}^{\frac{1}{2}}$$

e : 4.8 x 10<sup>-10</sup> [stat coulomb]

ε : 11.8

 $\hbar\omega$ : 1.17 [ev] = 1.17 x 1.6 x 10<sup>-19</sup> x 10<sup>7</sup> [erg]

m : 0.072 m

m<sub>V</sub>\*: 0.68 m

 $m_{V_2}^*$ : 0.085 m

 $m : 9.1 \times 10^{-28} [g]$ 

 $m_{cV_{i}}^{*}: \frac{m_{c}^{*} m_{V_{i}}^{*}}{m_{c}^{*} + m_{V_{i}}^{*}}$ 

 $\frac{|(\hat{P} \cdot \overline{\alpha})_{cV_{\hat{1}}}|}{m^2} = \frac{3E_3}{2m_c^*}$ 

 $E_8 = 1.51$  [ev] = 1.51 x 1.6 x 10 <sup>19</sup> x 10<sup>7</sup> [erg] at 77°K

Substitute these values

Then 
$$d = 0.15$$
  $\left[\frac{\text{cm} \cdot \text{sec}}{\text{erg}^2}\right]$ 

Two photon absorption coefficient K is 2ħωaI

$$K = 2 \times 1.17 \times 1.6 \times 10^{-19} \times 10^7 \times 0.15 \times I$$
 where I is in  $\left[\frac{\text{erg}}{\text{cm}^2 \cdot \text{sec}}\right]$ 

Thus

$$K^{23} = 2 \times 1.17 \times 1.6 \times 10^{-12} \times 0.15 \times 1 \times 10^{7} \times 10^{6}$$

where I is in 
$$\left[\frac{MW}{cm^2}\right]$$
.

If we assume 
$$I = 1 \left[ \frac{MW}{cm^2} \right]$$
,

$$K^{(a)} = 5.6 \left[ \frac{1}{cm} \right]$$

#### APPENDIX III

# SOLUTION OF DIFFERENTIAL EQUATION

$$\frac{dI}{dX} = -2\hbar\omega W - KI$$

Note that 
$$W = W^{(2)}$$
 and  $K = K^{(1)}$ .

$$\frac{dI}{dX} = -2\hbar\omega W - KI = -2\hbar\omega \partial_{x} I^{2} - KI$$

Let 2ħω a=β

$$\frac{dI}{dX} = -\beta I^2 - I$$

$$\frac{dI}{dX} = -\beta(I^2 + \frac{K}{\beta}I)$$

$$\frac{dI}{I(I+\frac{K}{\beta})} = -\beta dX$$

$$\int_{I_0}^{I} \frac{dI}{I(I+\frac{K}{\beta})} = - \int_{0}^{X} dX$$

$$\frac{\beta}{K} \ln \frac{I}{I + \frac{K}{\beta}} \Big|_{I_0} = -\beta X$$

$$\ln \left( \frac{I}{I + \frac{K}{\beta}} / \frac{I_0}{I_0 + \frac{K}{\beta}} \right) = -KX$$

$$\frac{I}{I+\frac{K}{B}} = \frac{I_0}{I_0+\frac{K}{B}} e^{-KX}$$

$$\frac{I}{\frac{K}{B}} = \frac{I_0 e^{-KX}}{I_0 (1 - e^{-KX}) + \frac{K}{B}}$$

$$I = \frac{I_0 e^{-KX}}{1 + \frac{\beta}{K} I_0 (1 - e^{-KX})}$$

when KX << 1

$$I(X) = \frac{I_0}{2\hbar\omega a I_0 X + 1}$$

Hence,

$$I = \frac{I_0 \exp(-KX)}{1 + \frac{\beta}{K} I_0 [1 - \exp(KX)]}$$

$$= \frac{I_0}{1 + \frac{\beta}{K} I_0 [1 - (1-KX)]}$$

$$= \frac{I_0}{1 + \beta I_0 X}$$

#### APPENDIX IV

## ADJUSTMENT OF Nd:glass LASER

There are important factors for lasing of Nd:glass mode locked laser.

At first, even though all components of the laser were arranged according to estimation and calculation, it was not easy to get good laser pulse. In order to improve lasing, a great deal of attention should be paid to the following factors.

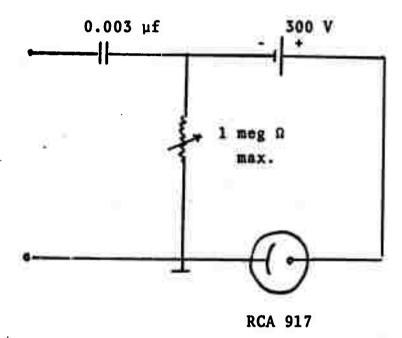
- 1. Microscale alignment of the equipments
- 2. Operating voltage of pumping flash lamp
- 3. Concentration of dye.

According to the experience, it was not difficult to estimate the operating level of voltage and the concentration of dye. To accomplish part 1., first it was helpful to take burn pattern on dark photographic picture. That is, we could examine the spatial coherence of the laser beam. When the burn pattern was not good, we tried same thing after adjusting venier of mirror mount. Repeating those procedures it was possible to get good shape of pulses. In the experiment, it was necessary to have single envelope of pulse. If not, it was difficult to estimate the power. To get single pulse, the operating voltage should be just above the threshold.

Difficulty occurred when the threshold came down. This was because the light from flash lamp might deteriorate the function of bleachable dye. In that case, it was needed to adjust the operating voltage. For the experiment of spectral response of GaAs, it was required to keep power level constant, so instead of adjusting operating voltage, we added dye a little bit to keep threshold constant.

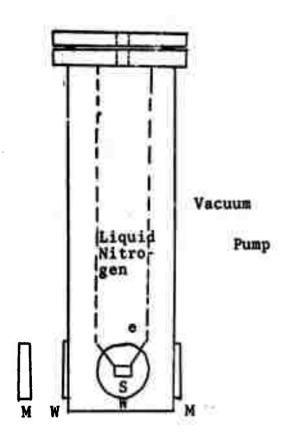
# APPENDIX V

# CIRCUIT DIAGRAM OF DETECTOR



# APPENDIX VI

## DEWER



M: Mirror

W: Window

C: Cold finger

S: Sample (GaAs)

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